S&P Systematic Global Macro Index (S&P SGMI) Methodology
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Introduction

Index Objective and Overview

The S&P Systematic Global Macro Index (S&P SGMI) measures the performance of a strategy based on price trends of specific globally traded liquid future contracts by tracking long, short, or zero positions. The strategy is designed to represent the general level of volatility taken by managers in the global macro and managed futures/Commodity Trading Advisor (CTA) universe, while still being subject to leverage constraints.

Highlights

The index follows a quantitative methodology to track the prices of a globally diversified portfolio of over three dozen commodity, foreign exchange, and financial futures contracts. Each contract (also called a constituent) may be in a long, short, or no investment position depending upon a trend signal generated by a regression of its historical prices, as outlined in Appendix A: Rebalancing Procedures.

The index is composed of 37 constituents determined every two years and grouped into six significant sectors traded in the global macro universe. Each sector is allocated an equal risk capital allowance with the underlying constituents within each sector evenly weighted as well. The resulting hypothetical portfolio is then leveraged in such a way that the effects of diversification among the various constituents are taken into account. Finally, the weights are adjusted to fit within the leverage constraints. Sectors and constituents are rebalanced monthly.

The S&P SGMI was developed collaboratively by S&P Dow Jones Indices and Thayer Brook Partners, LLP. The index is calculated and managed independently by S&P Dow Jones Indices according to S&P Dow Jones Indices’ standard policies and procedures, including the policies and procedures governing S&P Dow Jones Indices’ independent Index Committee.

Index Family

S&P Dow Jones Indices also calculates two standalone sub-indices representing the components of the S&P SGMI. These are the S&P SGMI Commodity (reflecting the physical commodity futures components of the S&P SGMI) and the S&P SGMI Financial (reflecting the financial futures components of the S&P SGMI) Indices. Excess and Total Return sub-indices are calculated and published for each of these two market sectors. The S&P SGMI Commodity and S&P SGMI Financial indices are completely independent standalone indices that follow the S&P SGMI methodology.

Supporting Documents

This methodology is meant to be read in conjunction with supporting documents providing greater detail with respect to the policies, procedures and calculations described herein. References throughout the methodology direct the reader to the relevant supporting document for further information on a specific topic. The list of the main supplemental documents for this methodology and the hyperlinks to those documents is as follows:

<table>
<thead>
<tr>
<th>Supporting Document</th>
<th>URL</th>
</tr>
</thead>
<tbody>
<tr>
<td>S&amp;P Dow Jones Indices’ Index Mathematics Methodology</td>
<td>Index Mathematics Methodology</td>
</tr>
</tbody>
</table>

S&P Dow Jones Indices: S&P Systematic Global Macro Index (S&P SGMI) Methodology
This methodology was created by S&P Dow Jones Indices to achieve the aforementioned objective of measuring the underlying interest of each index governed by this methodology document. Any changes to or deviations from this methodology are made in the sole judgment and discretion of S&P Dow Jones Indices so that the index continues to achieve its objective.
Index Constituents and Weightings

Eligibility

The Contracts included in the S&P SGMI are determined every two years and must satisfy several eligibility criteria. First, S&P Dow Jones Indices identifies those contracts that meet the general criteria for eligibility. Second, the Contract liquidity requirements are applied. The list of Designated Contracts for the relevant S&P SGMI Years is, then, complete and the process moves to the determination of the constituents’ weights discussed below.

Physical Commodity, Financial, and Foreign Exchange Futures. To be eligible for inclusion in the S&P SGMI, a Contract must be on a physical commodity, bond, currency, interest rate or an equity index. The Contracts need not require physical delivery by their terms in order for a commodity to be considered a physical commodity.

Certain Contract Characteristics. In order for a Contract to be eligible for inclusion in the S&P SGMI, the following criteria must be satisfied: (i) the Contract must have a specified expiration or term, or provide in some other manner for delivery or settlement at a specified time, or within a specified time period, in the future; (ii) the Contract must, at any given point in time, be available for trading at least five months prior to its expiration or such other date or time period specified for delivery or settlement.

Denomination and Geographical Requirements. To be eligible for inclusion in the S&P SGMI, a Contract must be traded on or through a Trading Facility that has its principal place of business or operations in a country that is a member of the Organization for Economic Cooperation and Development (OECD) during the relevant Annual Calculation Period or Interim Calculation Period.

Availability of Daily Contract Reference Prices. For a Contract to be eligible for inclusion in the S&P SGMI, Daily Contract Reference Prices generally must have been available on a continuous basis for at least two years prior to the proposed date of inclusion. In certain situations, if a new Contract is identified, S&P Dow Jones Indices may determine its inclusion over a shorter time period if sufficient historical Daily Contract Reference Prices for the given Contract can be derived from Daily Contract Reference Prices of a similar or related Contract.

Such publication must include, at all times, Daily Contract Reference Prices for at least one Contract Expiration that is five months or more from the date the determination is made, as well as for all Contract Expirations during such five-month period.

Availability of Volume Data. For a Contract to be eligible for inclusion in the S&P SGMI, volume data must be available for at least two years immediately prior to the date on which the determination to include the contracts is made. The S&P SGMI determination date is the same as the S&P GSCI for annual volume data, the 12-month periods from September through August.

Other Requirements with respect to the Trading Facility. The Trading Facility on or through which a Contract is traded must (i) make price quotations generally available to its members or participants (and to S&P Dow Jones Indices) in a manner and with a frequency that is sufficient to provide reasonably reliable indications of the level of the relevant market at any given point in time; (ii) make reliable trading volume information available to S&P Dow Jones Indices with at least the frequency required by S&P Dow Jones Indices to make the monthly determinations described under Sources of Information below.
Liquidity Requirement

The S&P SGMI is limited to those Contracts that are actively traded in order to assure that the prices generated by the markets for such Contracts represent reliable, competitive prices. Liquidity is determined by the annual Total Dollar Value Traded (TDVT). The Contracts that satisfy the general eligibility requirements set forth in General Eligibility Requirements above must, therefore, also satisfy the liquidity requirements described below before being included in the S&P SGMI. Exhibit 1 on the following page displays the most liquid contracts from each sector that are included according to these criteria.

EXHIBIT 1: CONTRACT INCLUSION CRITERIA

<table>
<thead>
<tr>
<th>Sector</th>
<th>Constituent</th>
<th>Exchange</th>
<th>Sector</th>
<th>Currency</th>
<th>Inclusion Criteria</th>
<th>TDVT&gt;$5B</th>
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<td>E</td>
<td>USD</td>
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<td>Top 6</td>
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<td>USD</td>
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<tr>
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<td>E</td>
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<td>Wheat</td>
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<td><strong>Commodity - Metals</strong></td>
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<td>Gold (100 oz.)</td>
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<td>T-Notes (10-year)</td>
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<td>CME</td>
<td>FX</td>
<td>USD</td>
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<td>Top 6 US</td>
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<td>Japanese Yen</td>
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<td>Australian Dollar</td>
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<td>Canadian Dollar</td>
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<td>Swiss Franc</td>
<td>CME</td>
<td>FX</td>
<td>USD</td>
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<td><strong>Equity - U.S.</strong></td>
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<td>S&amp;P 500 Index Complex</td>
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<td>USD</td>
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<td>Euro Stoxx 50</td>
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<td><strong>Equity - Asia</strong></td>
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<td>SI</td>
<td>JPY</td>
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</table>
The S&P SGMI Select Sectors

The six S&P SGMI sectors are categorized into two subsets: the financial select sector and the commodities select sector. For each of these two select sectors, sub-indices are computed using the same methodology as the S&P SGMI. Exhibit 2 shows the various parameters for the S&P SGMI composite and select sectors indices.

EXHIBIT 2: COMPARISON

<table>
<thead>
<tr>
<th>Sector</th>
<th>Constituent</th>
<th>Exchange</th>
<th>Sector</th>
<th>Currency</th>
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<tbody>
<tr>
<td>STIR*</td>
<td>4th Quarterly Contract in each region</td>
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<td>STIR - U.S.</td>
<td>Eurodollars (3-month)</td>
<td>CME</td>
<td>STIR</td>
<td>USD</td>
</tr>
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<td>STIR - Europe</td>
<td>3 Month Euribor</td>
<td>LIFFE</td>
<td>STIR</td>
<td>EUR</td>
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<tr>
<td>STIR - Asia</td>
<td>3 Month Euroyen</td>
<td>TFX</td>
<td>STIR</td>
<td>JPY</td>
</tr>
</tbody>
</table>

*STIR stands for Short Term Interest Rate

The four sectors included in the S&P SGMI Financials are Equity, Fixed Income, Foreign Exchange and Short Term Interest Rates (STIR). There are six constituents in each of the Equity, Fixed Income and Foreign Exchange sectors, and three constituents in STIR. The two sectors included in the S&P SGMI Commodities are Energy and Commodities. There are six constituents in the Energy sector, and ten constituents in the Commodities sector.

Within each of the sub-indices, the risk capital allocations are carried out evenly first at the sector level, then again evenly within the individual constituents, in accordance with the S&P SGMI methodology.

Position Direction

In order to reflect the measure of the global macro and managed futures/Commodity Trading Advisor (CTA) universe, the S&P SGMI must take directional positions that are long or short in order to represent the positions of the general market. If there is a positive trend, then the position will be long; conversely, if there is a negative trend, then the position will be short.

Determining whether the trend is positive or negative for each constituent each month is dependent upon a series of steps that must be followed to develop a valid time-series regression model where the slope (positive/negative) acts as the position direction (long/short) indicator.

In order to establish whether a constituent is currently in an upward or downward trend we compute a linear regression of the constituent returns against time. If the regression line has a positive slope then the conclusion is that the market is currently trending upwards, and if the slope of the regression line is negative then the conclusion is that the market is trending downwards.
The first step in developing a constituent’s valid time series regression is to collect its daily historical price data and calculate a cumulative return for each day. At least 256 data points must be available or else the weight cannot be calculated, so there would be no position. However, since a historical return is often dependent on the prior return, known as autocorrelation, the return data alone is not sufficient to produce a valid model with a constant mean and variance. For example, the mean and variance may be increasing over time in an unadjusted model, so that any predicted value will be too low. Because the time trend may vary through history, the analysis will use only the most recent period when the trend was stable. To determine this time period an initial assumption is made that the trend was stable over the most recent 22 days, and then tests in five-day increments until the longest stability period is discovered.

To check for stability, the hypothesis that two variances are equal is tested. Equality indicates a stable trend and the longest period of stability ending with the current date is used for the position direction decision. The two variances are (1) the variance of the daily returns and (2) the variance of residuals of an Ordinary Least Squares (OLS) linear regression of the cumulative return \( y \) on time \( t \).

The statistical test that we use to test the validity of the linear regression model is the F-test (or variance ratio test), which tests whether the variance of the linear regression residuals (adjusted for autocorrelation) is the same as the variance of the first differences of cumulative returns series. This is the null hypothesis.

Equality of variances indicates that the linear regression model is a good fit for the data. If the variance of the residuals (adjusted for autocorrelation) is significantly larger than the variance of the first differences then this indicates that the linear model is not a good fit for the data which is likely to be due to non-linearity (e.g. a change in the trend). If the test cannot reject the null hypothesis that the two variances are equal, the time period is increased by five days and the variances are recomputed and retested. If the null hypothesis is rejected, indicating the variances are not equal, then the sign of the slope coefficient in the regression is used to determine the position: positive = long, negative = short and 0 = no position.

Again, as the residuals are likely to be auto-correlated an uncorrected F-test is oversensitive. To correct for this oversensitivity, the variance of the residuals are adjusted by a factor of \( 1 - \rho^2 \) where \( \rho \) is the autocorrelation lag at 1. Once F is too large, the regression is no longer as good at de-trending as the first differences, showing the residuals have more noise than the series itself. The autocorrelation of the residuals is computed as follows:

\[
\rho = \frac{1}{(n-1)} \sum_{t=1}^{n-1} (y_t - \mu)(y_{t+1} - \mu) \left/ \text{Var}(y_t) \right. + (1/n)
\]

where:
- \( y_t \) = the residual at time \( t \)
- \( \mu \) = the mean of the residuals \( (1.., n) \), and
- \( n \) = the number of days in the relevant period.
- \( 1/n \) is included to correct for a negative bias in the autocorrelation of a short time series. As the time series gets longer, this term becomes less relevant.

\( F \) is then defined as:

\[
F = \frac{\text{Var(residuals)} \times (1 - \rho^2)}{\text{Var(FD)}}
\]

where

\( FD \) = the first differences of the daily cumulative percentage return series used in the regression.
\( \text{residuals} \) = residuals of the OLS.
Finally, the iterative process based on the continuous cumulative component returns and a confidence interval of 95% is run to establish the direction based on the slope of the regression. This is referred to as the F-Inverse function \( F_{inv} \). The process starts at the present and works backwards until:

\[
F > F_{inv}(95\%, n-3, n-2)
\]

where \( n \) = the number of days looking back

note: the F-Inverse function is rounded to 2 decimal places to assure that the algorithm is easily repeatable.

More specifically, the algorithm starts by regressing the past 22 days, beginning with the rebalancing reference date. If \( F < F_{inv}(95\%, 19, 20) \), the process continues by adding five days of history with each iteration until \( F > F_{inv}(95\%, n-3, n-2) \).

Once \( F > F_{inv}(95\%, n-3, n-2) \), the sign of the slope determines the market position. If the slope is negative (downward sloping) then the market position for that component is short. Conversely, if the slope is positive (upward sloping) then the market position for that component is long.

*For more information on position direction, please refer to the Appendix.*

**Weighting Scheme**

The intention of the S&P SGMI weighting scheme is to create an index where each of the sectors is allocated the same risk capital allowance, with each of the constituents allocated the same risk capital allowance within its sector. The idea is that no single sector or constituent should drive the volatility of the index.

It is important to note that the goal of the weighting methodology is to allocate the risk capital allowance as evenly as possible. The S&P SGMI is a leveraged product and, as such, is not trying to minimize volatility for a given investment. It has been specifically designed to be mathematically valid without being overly dependent on the individual elements of the cross-correlation matrix. The S&P SGMI methodology creates a consistent and efficient portfolio by first producing a set of relative weights which creates the diversified portfolio. To take advantage of this diversification, leverage management then occurs by scaling the portfolio to the target volatility by using a factor which is solely dependent upon the overall average of the cross-correlation matrix and not the individual elements of that matrix. The overall portfolio average is more stable than the individual elements and, thus, ultimately facilitates the calculation of a portfolio that is leveraged to achieve a given target volatility.

In order to apply this concept to the S&P SGMI, the number of contracts needs to be determined for each constituent, so it is necessary to choose a dollar amount and target index volatility. The dollar amount or assets under management (AUM) is arbitrary but the target volatility level is currently set to 17.5%, and is meant to represent the average volatility of the global macro managed futures/Commodity Trading Advisor (CTA) universe.

From the AUM and target volatility, a US$ daily risk allowance is calculated for the entire index by multiplying the AUM by the daily target volatility.

\[
US$ Daily Risk Allowance_{\text{Index}} = AUM_{US$} \times \frac{Target Volatility}{\sqrt{256}}
\]

It represents the total dollar risk the index is allowed to take in one day.
The next step is to determine the daily risk allowance for each constituent. Again, the idea is for each sector to have an equal dollar risk allowance where each constituent in the sector also has an equal dollar risk allowance.

\[
\text{US$ Daily Risk Allowance}_{\text{Constituent}} = \frac{\text{US$ Daily Risk Allowance}_{\text{Index}} \times (1/N) \times (1/M) \times CF}{N}
\]

where:
- \( N \) = number of sectors in the index
- \( M \) = the number of constituents in its sector
- \( CF \) = the correlation factor.

The correlation factor needs to be considered in order to properly assess the risk allowance for each constituent. If the correlations were not considered or were just assumed to be 1, then the daily risk allowance would be too low to hit the chosen target volatility. In order to compute the correlation factor, a correlation matrix of daily returns of all constituents is run and the average of the lower left triangle is calculated (AC).

\[
CF = \sqrt{\frac{Q}{1 + ((Q - 1) \times AC)}}
\]

which allows the index to allocate over the AUM (apply leverage) with the intention of reaching the target volatility.

where:
- \( Q \) = the number of total constituents in the index

Once each constituent’s US$ daily risk allowance is determined, the number of contracts needed to fill the position is calculated by dividing the daily risk allowance by the US$ dollar risk of one contract. For each constituent, the US$ dollar risk of one contract is measured by multiplying the standard deviation of the first differences of local prices by the local value of the contract tick and then by the exchange rate to the US$. So, all else being constant, higher volatility of a constituent will yield a higher US$ dollar risk of one contract so fewer contracts will be needed to fill the total risk allowance for the constituent. Conversely, if the volatility is too low, too many contracts would be required to fill the total risk allowance, or it might not be possible at all.

The index solution for this problem is to set a threshold of 0.125% as a lower limit to a ratio that tests whether there is enough volatility for the contract size.

\[
\text{Ratio} = \frac{\text{US$} \times \text{risk} \times m}{m \times P \times \text{tick} \times FX}
\]

where:
- \( \text{US$} \times \text{risk} \) = US$ risk per constituent contract
- \( m \) = number of contracts
- \( P \) = last local contract price
- \( \text{tick} \) = the local value of a contract tick
- \( FX \) = exchange rate to the US$

Note: the denominator in the equation above measures the nominal value of the constituent in US$.

If this ratio is less than 0.125%, then no position is taken so the weight of the constituent will be zero.
Again, since the correlation factor allows for an allocation greater than the AUM, also known as leverage, the index needs to adjust so that the leverage is never greater than 3x or 300% total nominal exposure. If the total nominal exposure of the index is greater than 300%, then 300% is divided by the total nominal exposure of the index to create a scale-back factor. This ratio will be applied to the number of contracts for each constituent to reduce the index to 300% of total nominal exposure.

Please see the formulas below that show the mathematical concept behind using the Correlation Factor (CF) in the weighting scheme. This illustration is for the simplified case where all individual constituents are allocated equally, which differs slightly from the adopted allocation scheme. Although the model is not exact, our studies show that the practical benefits derived from correlation stability far outweigh the mathematical rigor of a full-scale model.

By definition, the variance of the portfolio returns is determined as the sum of the individual variances plus a cross-correlation factor. This is shown in the formula below:

$$\sum_{i=1}^{m} \text{Var}(x_i) + \sum_{i \neq j}^{m} \rho_{i,j} \sigma_i \sigma_j$$

where,

$\rho = \text{correlation}$

$\sigma = \text{standard deviation}$

$m = \text{number of constituents}$

Since each risk unit, by design, has the same expected standard deviation, the equation can be rewritten as:

$$m \text{Var}(x) + \text{Var}(x) \sum_{i \neq j}^{m} \rho_{i,j}$$

The equation for the portfolio variance can now be restated as:

$$m \text{Var}(x) \left(1 + \frac{1}{m} \sum_{i \neq j}^{m} \rho_{i,j}\right)$$

The size, $N$, of the correlation matrix is:

$$N = (m^2 - m) = m(m - 1)$$

Thus the average of the correlation matrix, $\bar{\rho}$, is given by the following identities,

$$\bar{\rho} = \frac{\sum_{i \neq j} \rho_{ij}}{N} = \frac{\sum_{i \neq j} \rho_{ij}}{m(m - 1)}$$

And so it follows that:

$$\frac{1}{m} \sum_{i \neq j} \rho_{ij} = \bar{\rho}(m - 1)$$

Substituting the above equation into the equation for the portfolio variance, we get:
\[ m \text{Var}(x)(1 + \rho(m - 1)) \]

And it follows that the scaling factor is only proportional to the average of the cross-correlation matrix:

\[ \frac{\text{Var}(\text{portfolio})}{m^2 \text{Var}(x)} = (1 + (m - 1)\bar{\rho}) / m \]
Therefore, the size of each risk unit can be computed directly from the target volatility:

\[
\text{Var}(x) = \left( \frac{\text{Var}(\text{portfolio})}{m^2} \right) \left( \frac{m}{1 + (m-1)\rho} \right)
\]

Or, taking the square root of this equation we arrive at:

\[
\sigma_{\text{per risk unit}} = \frac{\sigma_{\text{daily target}}}{m} \sqrt{\frac{m}{1 + (m-1)\rho}}
\]

Thus, the size of each risk unit is equal to the risk capital allocated to the constituent multiplied by the Correlation Factor (CF).

The number of contracts which can be traded to create a single risk unit is:

\[
\frac{\sigma_{\text{per risk unit}}}{\sigma_{\text{per contract}}}
\]

At the end of each month, the USD standard deviation of each component is sampled over the past 60 trading days, to yield the \(\sigma_{\text{per contract}}\) which is used with the preceding formula to determine the number of contracts in a risk unit for any given component.

According to the representative volatility of managers in the CTA universe as determined by TBP, the target S&P SGMI annualized volatility is set to 17.5%, before any restriction on exposure. If a component’s USD standard deviation divided by its nominal size is less than 0.125%, then there is no position for that contract. If the gross exposure of the index is greater than 300%, each contract is scaled back proportionately such that the overall gross exposure is 300%.

Thus, the number of contracts for any given component is computed using the formula:

\[
C = \left( \frac{17.5\%}{\sqrt{256}} \right) \frac{m}{\sqrt{1 + (m-1)\rho}}
\]

For more information on the weighting scheme, please refer to the Appendix.

Rebalancing

**Monthly Rebalancing for Component Weights.** Components are rebalanced according to the signals generated by the algorithm run after the close of the last business day of each month. The rebalancing reference position implementation period is the second (2nd) through the sixth (6th) S&P SGMI business days of the month.

**Bi-Annual Rebalancing for Component Weights.** At the beginning of every other year, each of the constituents is evaluated for liquidity to ensure only the most liquid is included in the index as determined by the TDVT.
Sources of Information

The following are the sources of the information used to determine the eligibility of Contracts for inclusion in the S&P SGMI pursuant to the requirements set forth in General Eligibility Requirements. If any of the sources identified below is unavailable, with respect to the determination of the S&P SGMI for a particular S&P SGMI Year, S&P Dow Jones Indices will identify appropriate alternative sources and the composition of the S&P SGMI for such year will be based on such alternative sources. In addition, if S&P Dow Jones Indices, in its reasonable judgment, believes that one or more of the sources identified below contains a manifest error, it may use an alternative source to obtain the necessary information. Any such alternative sources used by S&P Dow Jones Indices will be publicly disclosed at the time that the composition of the S&P SGMI for the next S&P SGMI Year is announced.

General Eligibility Requirements. The identification of those futures that satisfy the general eligibility requirements set forth in General Eligibility Requirements is based on (1) the FIA (Futures Industry Association) Reports that are published at the time of the relevant Annual Calculation Period or Interim Calculation Period, and (2) the most recent version of the Futures and Options Fact Book, published by the Futures Industry Institute. The determination as to whether a particular Trading Facility has its principal place of business or operations in an OECD country is based on the most recent data published by the OECD.

Contract Volume and Liquidity Requirements. In order to determine whether a particular Contract satisfies the volume and liquidity requirements described above, S&P Dow Jones Indices may use any available sources that it believes to be reasonably reliable including, but not limited to, data contained in the FIA Reports. In the event of manifest error, S&P Dow Jones Indices may supplement, and make corrections to, any such data.
Index Maintenance

The S&P SGMI is a strategy of capturing futures contract price trends even though futures contracts have limited durations. Consequently, for the indicator to be calculated through time it must change (or roll) from tracking contracts that are approaching expiration to tracking new contracts. Each contract has its own “roll pattern” based on historical liquidity as determined by the Total Dollar Value Traded (TDVT) and open interest.

Exhibit 3 is a schedule of the active contracts used for price inputs of the Index.

**EXHIBIT 3: SCHEDULE OF CONTRACT MONTHS**

<table>
<thead>
<tr>
<th>S&amp;P SGMI Designated Contract Roll Schedule - Designated contract month the index rolls into at the beginning of each month.</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Contract</strong></td>
</tr>
<tr>
<td>----------------</td>
</tr>
<tr>
<td>Australian Dollar</td>
</tr>
<tr>
<td>British Pound</td>
</tr>
<tr>
<td>Canadian Dollar</td>
</tr>
<tr>
<td>Euro</td>
</tr>
<tr>
<td>Japanese Yen</td>
</tr>
<tr>
<td>Swiss Franc</td>
</tr>
<tr>
<td>10 Year Note</td>
</tr>
<tr>
<td>Treasury Bond</td>
</tr>
<tr>
<td>5 Year Note</td>
</tr>
<tr>
<td>Coffee “C”</td>
</tr>
<tr>
<td>Sugar #11</td>
</tr>
<tr>
<td>Cotton #2</td>
</tr>
<tr>
<td>Crude Oil</td>
</tr>
<tr>
<td>Heating Oil</td>
</tr>
<tr>
<td>RBOB Gasoline</td>
</tr>
<tr>
<td>Natural Gas</td>
</tr>
<tr>
<td>Com</td>
</tr>
<tr>
<td>Soybeans</td>
</tr>
<tr>
<td>Wheat (Chicago)</td>
</tr>
<tr>
<td>NA Copper (COMEX)</td>
</tr>
<tr>
<td>Live Cattle</td>
</tr>
<tr>
<td>Gold</td>
</tr>
<tr>
<td>Silver</td>
</tr>
<tr>
<td>GasOil</td>
</tr>
<tr>
<td>Brent Crude</td>
</tr>
<tr>
<td>Euro-Bund</td>
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<tr>
<td>Euro-Bobl</td>
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<tr>
<td>Nasdaq 100 Index</td>
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<tr>
<td>S&amp;P 500 Index</td>
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<td>Euro Stoxx 50</td>
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<td>Dax</td>
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<tr>
<td>Kospi 200</td>
</tr>
<tr>
<td>Nikkei 225</td>
</tr>
<tr>
<td>Eurodollars (3-month)</td>
</tr>
<tr>
<td>Euriibor (3-month)</td>
</tr>
<tr>
<td>Euroyen (3-month)</td>
</tr>
</tbody>
</table>
EXHIBIT 4: MONTH LETTER CODES

<table>
<thead>
<tr>
<th>LETTER</th>
<th>CONTRACT EXPIRATION</th>
</tr>
</thead>
<tbody>
<tr>
<td>F</td>
<td>JAN</td>
</tr>
<tr>
<td>G</td>
<td>FEB</td>
</tr>
<tr>
<td>H</td>
<td>MAR</td>
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<tr>
<td>J</td>
<td>APR</td>
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<td>K</td>
<td>MAY</td>
</tr>
<tr>
<td>M</td>
<td>JUN</td>
</tr>
<tr>
<td>N</td>
<td>JUL</td>
</tr>
<tr>
<td>Q</td>
<td>AUG</td>
</tr>
<tr>
<td>U</td>
<td>SEP</td>
</tr>
<tr>
<td>V</td>
<td>OCT</td>
</tr>
<tr>
<td>X</td>
<td>NOV</td>
</tr>
<tr>
<td>Z</td>
<td>DEC</td>
</tr>
</tbody>
</table>

The risk of aberrational liquidity or pricing of a commodity futures contract around the maturity date is greater than in the case of cash-settled futures contracts because (among other factors) a number of market participants take delivery of the underlying commodities. Spot markets in commodities occasionally have delivery problems related to, for example, weather conditions disrupting transportation of cattle to a delivery point. Such a delay could cause the spot market to move significantly, while latter-dated futures contracts are little changed. The strategy avoids delivery issues by owning contracts that are outside of nearby delivery.

Currency of Calculation and Additional Index Return Series

The S&P SGMI is calculated in U.S. dollars. The prices of the underlying futures contracts are collected in their local currencies. Using WM/Refinitiv’s spot exchange rates, these local prices are converted to U.S. dollars.

Real-time Forex rates, as supplied by WM/Refinitiv, are used for ongoing index calculation. The index’s final closing values convert all underlying contracts prices used in the index calculation at the spot exchange rates provided by WM/Refinitiv at 04:00 PM London Time.

In addition to the indices detailed in this methodology, additional return series versions of the indices may be available, including, but not limited to: currency, currency hedged, decrement, fair value, inverse, leveraged, and risk control versions. For a list of available indices, please refer to the S&P DJI Methodology & Regulatory Status Database.

For information on index calculation, please refer to S&P Dow Jones Indices’ Index Mathematics Methodology.

For the inputs necessary to calculate certain types of indices, including decrement, dynamic hedged, fair value, and risk control indices, please refer to the Parameters documents available at www.spdji.com.
Index Calculation

Please note, for all calculations below the formulae include the contract rolls that occur during the monthly rebalancings. During the remainder of each month, only one contract will be in effect, so the irrelevant portions of some equations will not apply.

Spot Calculation

On a given S&P SGMI business day, \( d \), the spot price \( (SPOT) \) of the index containing \( i \) number of Components (\( c \)) is calculated as follows:

\[
SPOT_d = \left( \frac{\sum_{c=1}^{i} TDW_1 + SC1}{NC_{old}} \right) + \left( \frac{\sum_{c=1}^{i} TDW_2 + SC2}{NC_{new}} \right)
\]

where

\[
\sum_{c=1}^{i} TDW_1 = \text{The sum of the Total Dollar Weight (TDW) of each Component’s (c’s) Current Contract.}
\]

\[
\sum_{c=1}^{i} TDW_2 = \text{The sum of the TDW of each Component (c’s) next Contract}
\]

\[SC1 = \text{The Short Component effective during the last month, expressed in the same terms as the Contract Weights, CWs.}\]

\[SC2 = \text{The Short Component effective in the current month, expressed in the same terms as the CWs.}\]

\[NC_{old} = \text{Normalizing Constant effective during the last month}\]

\[NC_{new} = \text{Normalizing Constant effective during this month}\]

The Short Component (\( SC \)) is allocated to the amount of weight remaining in the Index after the weights of each component has been defined based on the long and short positions and their respective percentage weights. Adding the weight of the Short Component to the sum of the weights of the Components makes the weight in the Index sum to 100%.
The Short Component is calculated as follows:

\[ SC = \text{Number of Contracts} \times CRW_{cd} \times \text{Position} \]

where

\[ CRW_{cd} = \text{Contract Roll Weights for Future } c \text{ on day } d \]

\[ \text{Position is set as defined in the Appendix.} \]

\[ \text{Please see the contract roll weights table on the next page for the CRW on day } d. \]

**Total Dollar Weight Calculation**

On a given S&P SGMI business day, \( d \), the Total Dollar Weight (TDW) for Future \( c \) is the product of its Contract Weight, Contract Roll Weight, Daily Contract Reference Price and US$ exchange rate for the current and next contracts, respectively.

\[
TDW_{cd} = \sum_{i=1}^{i} TDW_{c_{d-1}} \times (CRW_{c_{d}} / CRW_{c_{d-1}}) + (CW_{c_{d}} \times CRW_{c_{d}} \times (DCRP_{c_{d}} - DCRP_{c_{d-1}}) \times FX_{c_{d}})
\]

On the roll start date for the contract rolling in and on the base date for the contract rolling out, the TDW is as follows:

\[
TDW_{c_{d}} = CW_{c_{d}} \times CRW_{c_{d}} \times DCRP_{c_{d}} \times FX_{c_{d}}
\]

After the completion of the roll, for the current contract, the TDW is as follows:

\[
TDW_{c_{d}} = \sum_{i=1}^{i} TDW_{c_{d-1}} + (CW_{c_{d}} \times CRW_{c_{d}} \times (DCRP_{c_{d}} - DCRP_{c_{d-1}}) \times FX_{c_{d}})
\]

where

\[ TDW_{c_{d}} = \text{Total Dollar Weight for Future } c \text{ on day } d. \]

\[ TDW_{c_{d-1}} = \text{Total Dollar Weight for Future } c \text{ on the S&P SGMI business day prior to day } d. \]

\[ CW_{c_{d}} = \text{Contract Weight for Future } c \text{ set on day } d. \]

\[ CRW_{c_{d}} = \text{Contract Roll Weights for Future } c \text{ on day } d \]

\[ CRW_{c_{d-1}} = \text{Contract Roll Weights for Future } c \text{ on the S&P SGMI business day prior to day } d. \]

\[ DCRP_{c_{d}} = \text{Daily Contract Reference Price for Future } c \text{ on day } d \]

\[ DCRP_{c_{d-1}} = \text{Daily Contract Reference Price for Future } c \text{ on the S&P SGMI business day prior to day } d. \]

\[ FX_{c_{d}} = \text{Foreign Exchange Rate for Future } c \text{ on day } d \]

**Contract Weight**

Contract Weights (CWs) are determined on the last S&P SGMI business day of each month. Effective for the following roll start date. The CW value is calculated as follows:

\[ CW = \text{Multiplier} \times \text{Number of Contracts} \times \text{Position} \]

\[ \text{Multiplier = the value of a point} \]

\[ \text{For determination of the Number of Contracts and Position please refer to the Appendix.} \]
Contract Roll Weights Logic

On a given non-roll day, \( CRW_1 = 1 \) and \( CRW_2 = 0 \)

During the Roll Period the CRW value is computed as follows:

For the S&P SGMI the number of roll days is five (5).

\[
CRW = \frac{100\%}{\text{number of roll days}} = 20\%
\]

Since the number of roll days is five, 20% of its component will roll in and roll out daily, keeping the aggregate Component’s weight total of 100%.

<table>
<thead>
<tr>
<th>day ( d )</th>
<th>CRW1</th>
<th>CRW2</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.8</td>
<td>0.2</td>
</tr>
<tr>
<td>2</td>
<td>0.6</td>
<td>0.4</td>
</tr>
<tr>
<td>3</td>
<td>0.4</td>
<td>0.6</td>
</tr>
<tr>
<td>4</td>
<td>0.2</td>
<td>0.8</td>
</tr>
<tr>
<td>5</td>
<td>0</td>
<td>1.0</td>
</tr>
</tbody>
</table>

Normalizing Constant

In order to assure continuity of the S&P SGMI and to allow comparisons of the value of the S&P SGMI to be made over time, it is necessary to make an adjustment to the calculation of the S&P SGMI each time the CWs are changed. The factor used to make this adjustment is the Normalizing Constant (NC) and is used in the same manner as similar factors applied to the calculation of other published financial market indices. The NC is determined each time the composition of the S&P SGMI is changed pursuant to the procedures set forth in this methodology.

\[
NC_{\text{new}} = NC_{\text{old}} \times \frac{\sum (CW_2 \times DCRP_{1_d} + CW_2 \times DCRP_{2_d}) + SC_1}{\sum (CW_1 \times DCRP_{1_d} + CW_1 \times DCRP_{2_d}) + SC_2}
\]

where

\[
\begin{align*}
CW_1 &= \text{Last month’s Contract Weight} \\
CW_2 &= \text{This month’s Contract Weight} \\
SC_1 &= \text{Short Component effective during the last month, expressed in the same terms as Contract Weights, CWs} \\
SC_2 &= \text{Short Component effective in the current month, expressed in the same terms as CWs} \\
DCRP_{1_d} &= \text{Current contract price on day } d \\
DCRP_{2_d} &= \text{Next contract price on day } d \\
NC_{\text{old}} &= \text{Normalizing Constant effective as of the last month}
\end{align*}
\]

Excess Return Calculation

On a given S&P SGMI business day, \( d \), the S&P SGMI Excess Return (ER) index level is equal to the product of the S&P SGMI ER index level on the immediately preceding S&P SGMI business day and
multiplied by one plus the Contract Daily Return as of that day. The Index is calculated to a seven (7) digit precision.

\[
ER_d = ER_{d-1} \times [1 + CDR_d]
\]

where

- \(ER_d\) = Excess Return Value for S&P SGMI Business Day \(d\).
- \(ER_{d-1}\) = Excess Return Value as on the S&P SGMI business day prior to day \(d\).
- \(CDR_d\) = Contract Daily Return of the Index on the S&P SGMI business day prior to day \(d\).

**Contract Daily Return Calculation**

The Contract Daily Return (CDR) on any S&P SGMI Business Day, \(d\), is equal to the ratio obtained by dividing the Total Dollar Weight Obtained by the Total Dollar Weight Invested on the immediately preceding S&P SGMI Business Day, minus one.

\[
CDR_d = \frac{TDWO_d}{TDWI_d} - 1
\]

where

- \(TDWO_d\) = Total Dollar Weight Obtained for S&P SGMI Business Day \(d\).
- \(TDWI_d\) = Total Dollar Weight Invested for S&P SGMI Business Day \(d\).

**Total Dollar Weight Obtained**

On a given S&P SGMI business day, \(d\), the Total Dollar Weight Obtained (TDWO) is the amount obtained from an investment on the immediately preceding day. The TDWO for a given day is calculated using the Component Weights and Contract Roll Weights in effect on the immediately preceding day, \(d-1\), and the Daily Contract Reference Prices used to calculate the S&P SGMI Index on day \(d\).

\[
TDWO_d = \frac{NC_{new}}{NC_{old}} \times (TDWI_{1d} + TDWO_{2d})
\]

\[
TDWO_{1d} = \sum_{c=1}^{i} (TDW_{1d} - 1 + (CW_{1d} \times CRW_{1cd} - 1 \times (DCRP_{1cd} - DCRP_{1cd - 1}) \times FX_{cd}) + SC1
\]

\[
TDWO_{2d} = \sum_{c=1}^{i} (TDW_{2d} - 1 + (CW_{2cd} \times CRW_{2cd} - 1 \times (DCRP_{2cd} - DCRP_{2cd - 1}) \times FX_{cd}) + SC2
\]

where

- \(TDWO_{1d}\) = Total Dollar Weight Obtained of the current contract on day \(d\)
- \(TDWO_{2d}\) = Total Dollar Weight Obtained of the next contract on day \(d\)
- \(CW_{1d}\) = Contract Weight of the current contract on day \(d\)
Total Dollar Weight Invested

On a given S&P SGMI business day, \(d\), the Total Dollar Weight Invested (TDWI) is equal to the Total Dollar Weight of the immediate preceding S&P SGMI business day \(d-1\) and is calculated as follows:

\[
TDWI_d = \frac{NC_{new}}{NC_{old}} \cdot (TDWI_{1d} + TDWO_{2d})
\]

\[
TDWI_{1d} = \sum_{i=1}^{i} TDWI_{1d-1} + SC_1
\]

\[
TDWI_{2d} = \sum_{i=1}^{i} TDW_{2d-1} + SC_2
\]

where

- \(TDWI_{1d}\) = Total Dollar Weight Invested of the current contract on day \(d\)
- \(TDWI_{2d}\) = Total Dollar Weight Invested of the next contract on day \(d\)
- \(TDW_{1d-1}\) = Total Dollar Weight of of the current contract on the S&P SGMI business day prior to day \(d\).
- \(TDW_{2d-1}\) = Total Dollar Weight of the next contract on the S&P SGMI business day prior to day \(d\).
- \(SC_1\) = Short Component effective last month
- \(SC_2\) = Short Component effective in the current month.
- \(NC_{old}\) = Normalizing Constant effective as of the last month
- \(NC_{new}\) = Normalizing Constant effective during this month

Total Return Calculation

On any given calendar day, \(d\), the Treasury Bill Return (TBR) is equal to an amount determined in accordance with the following formula:
\[
TBR_d = \left[ \frac{1}{1 - \frac{91}{360} \times TBAR_{d-1}} \right]^{1/91} - 1
\]

where:

\( TBAR_{d-1} = \) The 3-month T-Bill Rate available on the S&P SGMI business day prior to day \( d \).

On a given S&P SGMI business day, \( d \), the value of the S&P SGMI Total Return (TR) Index is equal to the product of (i) the value of the S&P SGMI TR on the immediately preceding S&P SGMI Business Day, (ii) one plus the sum of the Contract Daily Return and the Treasury Bill Return on the day on which the calculation is made, and (iii) one plus the Treasury Bill Return for each non S&P SGMI Business Day since the immediately preceding S&P SGMI Business Day. The result of the foregoing calculation is, then, rounded to seven (7) digits of precision. The calculation of the S&P SGMI TR for any S&P SGMI Business Day, \( d \), is obtained by rounding the expression below to seven digits of precision.

\[
SPSGMITR_d = SPSGMITR_{d-1} \times (1 + CDR_d + TBR_d)^{*} \times (1 + TBR_d)^{days}
\]

where

\( SPSGMITR_{d-1} = \) S&P SGMI TR Index value on the S&P SGMI business day prior to day \( d \).
\( CDR_d = \) The Contract Daily Return on day \( d \).
\( TBR_d = \) Treasury Bill Return on day \( d \).
\( Days = \) Number of non-S&P SGMI business days since the last immediate preceding S&P SGMI Business Day.
## Glossary

<table>
<thead>
<tr>
<th>Term</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CDR</td>
<td>Contract Daily Return</td>
</tr>
<tr>
<td>CRW</td>
<td>Contract Roll Weight</td>
</tr>
<tr>
<td>CW</td>
<td>Contract Weight</td>
</tr>
<tr>
<td>DCRP</td>
<td>Daily Contract Reference Price</td>
</tr>
<tr>
<td>Active Contract</td>
<td>A liquid, actively traded Contract with respect to a Designated Contract, as defined or identified by the relevant Trading Facility or, if no such definition or identification is provided by the Trading Facility, as defined by standard custom and practice in the industry.</td>
</tr>
<tr>
<td>Contract Expiration</td>
<td>A date or term specified by the Trading Facility on or through which a Contract is traded as the date or term on, during or after which such Contract will expire, or delivery or settlement will occur. The contract expiration may, but is not required to, be a particular contract month.</td>
</tr>
<tr>
<td>NC</td>
<td>Normalizing Constant</td>
</tr>
<tr>
<td>Roll Period</td>
<td>With respect to any Designated Contract, the period of five S&amp;P SGMI Business Days beginning on the 2&lt;sup&gt;nd&lt;/sup&gt; S&amp;P SGMI Business Day of each calendar month and ending on the 6&lt;sup&gt;th&lt;/sup&gt; S&amp;P SGMI Business Day of such month.</td>
</tr>
<tr>
<td>ER Index</td>
<td>Excess Return Index, which is the accretion of the Contract Daily Return indexed to a normalized value</td>
</tr>
<tr>
<td>Spot Index</td>
<td>The index that reflects the price levels of the Designated Contracts and the CPW of each such Contract.</td>
</tr>
<tr>
<td>TR Index</td>
<td>The Total Return Index incorporates the returns of the ER Index and the Treasury Bill Return.</td>
</tr>
<tr>
<td>Treasury Bill Rate</td>
<td>Treasury Bill Rate (TBARd-1). On any S&amp;P SGMI Business Day, &lt;i&gt;d&lt;/i&gt;, the 91-day discount rate for U.S. Treasury Bills, as reported by the U.S. Department of the Treasury’s Treasury Direct service at <a href="http://www.treasurydirect.gov/RI/OFBills">http://www.treasurydirect.gov/RI/OFBills</a> on the most recent of the weekly auction dates prior to such S&amp;P SGMI Business Day, &lt;i&gt;d&lt;/i&gt;.</td>
</tr>
<tr>
<td>TDW</td>
<td>Total Dollar Weight</td>
</tr>
<tr>
<td>TDWO</td>
<td>Total Dollar Weight Obtained</td>
</tr>
<tr>
<td>TDWI</td>
<td>Total Dollar Weight Invested</td>
</tr>
<tr>
<td>TBR</td>
<td>Treasury Bill Rate</td>
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</table>
Index Governance

Index Committee

An S&P Dow Jones Indices’ Index Committee maintains the indices. All committee members are full-time professionals at S&P Dow Jones Indices. The Index Committee meets at a frequency it deems necessary. At each meeting, the Committee may review issues that may affect index constituents, statistics comparing the composition of the index to the market, commodities that are being considered as candidates for addition to the index, and any significant market events. In addition, the Index Committee may revise index policy covering rules for selecting commodities or other matters.

S&P Dow Jones Indices considers information about changes to its indices and related matters to be potentially market moving and material. Therefore, all Index Committee discussions are confidential.

S&P Dow Jones Indices’ Index Committees reserve the right to make exceptions, when applying the methodology if the need arises. In any scenario where the treatment differs from the general rules stated in this document or supplemental documents, clients will receive sufficient notice, whenever possible.

In addition to the daily governance of indices and maintenance of index methodologies, at least once within any 12-month period, the Index Committee reviews the methodology to ensure the indices continue to achieve the stated objectives, and that the data and methodology remain effective. In certain instances, S&P Dow Jones Indices may publish a consultation inviting comments from external parties.

For information on Quality Assurance and Internal Reviews of Methodology, please refer to S&P Dow Jones Indices’ Commodities Indices Policies & Practices Methodology.
Index Policy

Holiday Schedule

The S&P SGMI is calculated daily based on the same holiday schedule as the S&P GSCI which follows the official NYSE holiday schedule. The Index is calculated when the majority of the S&P SGMI futures contracts are open for official trading and official settlement prices are provided, excluding holidays and weekends.


Contact Information

For questions regarding an index, please contact: index_services@spglobal.com.
Index Dissemination

Index levels are available through S&P Dow Jones Indices’ Web site at [www.spdji.com](http://www.spdji.com), major quote vendors (see codes below), numerous investment-oriented Web sites, and various print and electronic media.

Tickers

The table below lists headline indices covered by this document. All versions of the below indices that may exist are also covered by this document. Please refer to the [S&P DJI Methodology & Regulatory Status Database](http://www.spdji.com) for a complete list of indices covered by this document.

<table>
<thead>
<tr>
<th>Index Description</th>
<th>Bloomberg Code</th>
<th>RIC Code</th>
<th>Base Date</th>
<th>Launch Date</th>
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</thead>
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<tr>
<td>S&amp;P Systematic Global Macro Commodities Index ER</td>
<td>SPSGMICP</td>
<td>.SPSGMICP</td>
<td>11/28/2003</td>
<td>02/24/2012</td>
</tr>
<tr>
<td>S&amp;P Systematic Global Macro Commodities Index TR</td>
<td>SPSGMICT</td>
<td>.SPSGMICT</td>
<td>11/28/2003</td>
<td>02/24/2012</td>
</tr>
<tr>
<td>S&amp;P Systematic Global Macro Financials Index ER</td>
<td>SPSGMIFP</td>
<td>.SPSGMIFP</td>
<td>11/28/2003</td>
<td>02/24/2012</td>
</tr>
<tr>
<td>S&amp;P Systematic Global Macro Financials Index TR</td>
<td>SPSGMIFT</td>
<td>.SPSGMIFT</td>
<td>11/28/2003</td>
<td>02/24/2012</td>
</tr>
<tr>
<td>S&amp;P SGMI Australian Dollar Long ER</td>
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<td>.SSGMLAP</td>
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<td>04/05/2016</td>
</tr>
<tr>
<td>S&amp;P SGMI United Kingdom Pound Long ER</td>
<td>SSGMBLP</td>
<td>.SSGMBLP</td>
<td>11/28/2003</td>
<td>04/05/2016</td>
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<tr>
<td>S&amp;P SGMI Canadian Dollar Long ER</td>
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<td>.SSGMOCT</td>
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<tr>
<td>S&amp;P SGMI Canadian Dollar Long TR</td>
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<tr>
<td>S&amp;P SGMI Euro Long ER</td>
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<tr>
<td>S&amp;P SGMI Switzerland Francs Long ER</td>
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<td>11/28/2003</td>
<td>04/05/2016</td>
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<tr>
<td>S&amp;P SGMI Switzerland Francs Long TR</td>
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<td>.SSGMSLT</td>
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<td>04/05/2016</td>
</tr>
<tr>
<td>S&amp;P SGMI Australian Dollar Long Short ER</td>
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<td>04/05/2016</td>
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<tr>
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<td>04/05/2016</td>
</tr>
<tr>
<td>S&amp;P SGMI United Kingdom Pound Long Short ER</td>
<td>SSGMBLSP</td>
<td>.SSGMBLSP</td>
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<td>04/05/2016</td>
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<tr>
<td>S&amp;P SGMI United Kingdom Pound Long Short TR</td>
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<td>04/05/2016</td>
</tr>
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<td>S&amp;P SGMI Canadian Dollar Long Short TR</td>
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</tr>
</tbody>
</table>

Index Data

Daily index levels and index data are available via subscription.

*For product information, please contact S&P Dow Jones Indices, [www.spdji.com/contact-us](http://www.spdji.com/contact-us).*

Web site

For further information, please refer to S&P Dow Jones Indices' Web site at [www.spdji.com](http://www.spdji.com).
Appendix A: Rebalancing Procedures

Index values and divisors are calculated every S&P SGMI business day. Along with the daily index calculations, the position determination and number of contracts (weights) calculations are made once a month on the Rebalancing Reference day.

Position Determination

Position refers to either a long, a short or no position for each futures contract. The position will be used for calculating each component’s daily Total Dollar Weight.

<table>
<thead>
<tr>
<th>Position Value</th>
<th>Position Type</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Long</td>
</tr>
<tr>
<td>-1</td>
<td>Short</td>
</tr>
<tr>
<td>0</td>
<td>No Position</td>
</tr>
</tbody>
</table>

For performing position determination S&P Dow Jones Indices requires at least 256 days of historic closing price data.

Steps for Position determination:

1. Beginning with the latest day, calculate the return for the contract for that date. The return is calculated by taking the current day’s \((t)\) contract closing price and calculating the return for it using the previous day’s \((t-1)\) closing price. During roll periods, contracts used in return calculations will change. For example, assuming we are rolling from a March to a June contract:

   On the Roll start date:
   \[
   Price\ Return_t = \frac{Price\ of\ March\ Contract_t - Price\ of\ March\ Contract_{t-1}}{Price\ of\ March\ Contract_t}
   \]

   On the day after the Roll:
   \[
   Price\ Return_t = \frac{Price\ of\ June\ Contract_t - Price\ of\ June\ Contract_{t-1}}{Price\ of\ June\ Contract_t}
   \]

2. Calculate the cumulative returns for each day using the formulae above.
3. Create a time-series of daily cumulative returns.
4. Take the last 22 cumulative returns and calculate the residuals from an Ordinary Least Square (OLS) regression curve.
5. Compute the autocorrelation adjusted variance of the residuals (AAVR).

\[
AAVR = \frac{\text{Variance of Residuals}}{\text{Residuals of Variance}} \left( 1 - \left( \frac{\text{Covariance of Residuals}}{\text{Variance of Residuals}} + \frac{1}{n} \right)^2 \right)
\]

This ratio is \(\rho\), the autocorrelation lag at 1.
6. Calculate the daily differences for the cumulative returns.
7. Calculate the variance of the differences calculated in step 6 for the 22 days over which the OLS was calculated.
8. Calculate the Variance Ratio using the AAWR and variance of differences calculated in steps 5 & 7.

\[ \text{Variance Ratio} = \text{AAWR} / \text{Variance of differences} \]

9. Calculate the F-Inverse function (FINV) using a probability = .05 (a 95% confidence interval), Degree of Freedom1 = \( n - 3 \) and Degree of Freedom2 = \( n - 2 \), where \( n = 22 \).
10. If \( \text{Variance Ratio} \leq \text{FINV} \) then increase the sample size by going back 5 more days and repeating steps 4 through 9
11. Once \( \text{Variance Ratio} > \text{FINV} \), then the breakpoint has been reached. The slope is calculated based on the cumulative returns from the breakpoint to the rebalancing reference day. The position value of a futures contract is, then, calculated using the Slope
   - If slope > 0, then Position Value = 1 (Long)
   - If slope < 0, then Position Value = -1 (Short)
   - If slope = 0, then Position Value = 0
12. If all historic contract prices are used and \( \text{Variance Ratio} \) is still less than \( \text{FINV} \) then the contract start date become the breakpoint. The slope and positions are calculated as mentioned in Step 11.

**Number of Contracts**

The following calculation is done once every month to determine the number of contracts for each index component.

1. The following parameters are used for the calculation of the number of contracts
   - i. Assets Under Management (AUM). This is a constant (US$ 10 billion) used to calculate the number of contracts. For example, a different number of contracts would be purchased in the index for US$ 10 million versus if there were US$ 100m. The weights will be the same, but the number of contracts will be different.
   - ii. Target Volatility (17.5%)
   - iii. Local Currency Per Unit for all futures contracts present in the index
   - iv. Threshold Floor (0.125%)
   - v. Threshold Ceiling (300%)
2. The following calculations are done to arrive at the number of contracts
   - i. \( \text{Volatility Per Day} = \frac{\text{Target Volatility}}{\sqrt{256}} \)
   - ii. \( \text{Daily Risk Allowance} = \text{Volatility Per Day} \times \text{AUM} \)
   - iii. Compute the average correlation factor using the last 256 daily returns of each instrument
   - iv. Calculate the standard deviation of the price differences for each instrument for the last 60 days
     - v. For each instrument,
US Dollar Risk = Local Currency Per Unit * Std Deviation of Price Differences * Fx Rate

vi. For each instrument,

\[ \text{Risk Allowance} = \text{Sector Weight} \times \text{Instrument Weight} \times \text{Daily Risk Allowance} \]

where

\[ \text{Sector Weight} = \frac{100\%}{\text{Number of Sectors}} \]

\[ \text{Instrument Weight} = \frac{\text{Sector Weight}}{\text{Number of Instruments in the Sector}} \]

vii. For each instrument,

\[ \text{Final Risk Allowance} = \text{Risk Allowance} \times \text{Correlation Factor (rounded to 1 decimal)} \]

viii. Contract Size = \( \frac{\text{Final Risk Allowance}}{\text{US Dollar Risk}} \); (rounded to 0 decimals)

ix. Nominal Value in Dollars = Local Currency Per Unit * Fx Rate * Contract Size * Instrument’s Last Closing Price

x. \( \frac{\text{Volatility Ratio}}{\text{Nominal}} = \frac{\text{US Dollar Risk} \times \text{Contract Size}}{\text{Nominal Value in Dollars}} \)

xi. If the \( \frac{\text{Volatility Ratio}}{\text{Nominal}} \) is less than the Threshold Floor then the Contract Size is 0, otherwise it is as calculated in step viii

xii. Nominal Value as a Percent of AUM = \( \frac{\text{Nominal Value in Dollars}}{\text{AUM}} \)

xiii. Total Nominal Exposure = \( \sum (\text{Nominal Value as a Percent of AUM}) \) for all futures in the index

xiv. If \( \text{Total Nominal Exposure} > \text{Threshold Ceiling} \) then,

- Scale Back = \( \frac{\text{Threshold Ceiling}}{\text{Total Nominal Value}} \), else
- Scale Back = 1
- Number Of Contracts = Scale Back * Contract Size; rounded to 0 decimals

**Cash Weight Calculation**

\[ \text{Cash Weight} = \text{AUM} - \text{Total Dollar Weight} \]

The Rebalancing Reference Day is the close of business of the last trading day of each month. The Rebalancing Day is the second trading day of each following month (this is also the contract Roll Start date).
Precisions for Calculation

The following are the precisions used for calculations

- OLS – 15 Decimals
- FINV – 2 Decimals
- Variance Ratio – 2 Decimals
- Correlation Factor – 1 Decimal
- Standard Deviation – 14 Decimals
- Contract Size (Instrument Weight) – Rounded to Nearest Whole Number
- Cash Weight – 14 Decimals
Appendix B: Long and Long Short Indices of Currency Futures Contracts

For each futures contract in the foreign exchange sector of the S&P SGMI, S&P Dow Jones Indices calculates two indices. One tracks the performance of holding the contract with a long only position, and the other with a long or short position – with the position determined on a monthly basis.

These indices are available for six currency futures that are included in the S&P SGMI’s foreign exchange sector: Australian Dollar (AUD), Canadian Dollar (CAD), Euro (EUR), Japanese Yen (JPY), Swiss Franc (CHF), and British Pound (GBP). The indices follow the same position determination and roll period as S&P SGMI.
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